

**Exercise 3. Integration using algebraic substitutions**

In Problems 1 to 6, integrate with respect to the variable.

$$1. \quad 2 \sin(4x + 9)$$

$$2. \quad 3 \cos(2\theta - 5)$$

$$3. \quad 4 \sec^2(3t + 1)$$

$$4. \quad \frac{1}{2}(5x - 3)^6$$

$$5. \quad \frac{-3}{(2x - 1)}$$

$$6. \quad 3e^{3\theta + 5}$$

In Problems 7 to 10, evaluate the definite integrals correct to 4 significant figures.

$$7. \quad \int_0^1 (3x + 1)^5 dx$$

$$8. \quad \int_0^2 x \sqrt{2x^2 + 1} dx$$

$$9. \quad \int_0^{\pi/3} 2\sin\left(3t + \frac{\pi}{4}\right) dt$$

$$10. \quad \int_0^1 3\cos(4x - 3) dx$$

**Exercise 4. Integration using algebraic substitutions**

In Problems 1 to 7, integrate with respect to the variable.

$$1. \quad 2x(2x^2 - 3)^5$$

$$2. \quad 5 \cos^5 t \sin t$$

$$3. \quad 3\sec^2 3x \tan 3x$$

$$4. \quad 2t\sqrt{3t^2 - 1}$$

$$5. \quad \frac{\ln \theta}{\theta}$$

$$6. \quad 3 \tan 2t$$

$$7. \quad \frac{2e^t}{\sqrt{e^t + 4}}$$

In Problems 8 to 10, evaluate the definite integrals correct to 4 significant figures.

$$8. \quad \int_0^1 3xe^{(2x^2 - 1)} dx$$

$$9. \quad \int_0^{\pi/2} 3 \sin^4 \theta \cos \theta d\theta$$

$$10. \quad \int_0^1 \frac{3x}{(4x^2 - 1)^5} dx$$